Math 250a (Fall '07) - Homework 10 extra problems

1. This problem is about the definite integral

$$\int_0^1 \sin^2(\pi x) \, dx$$

(a) Show the exact value of this integral is 1/2.

(b) Use the program to compute the trapezoid approximation for N = 10, 20 and 40. Find the error in each of the three cases.

(c) Use extrapolation with N = 10, 20 to find a better approximation and compute its error. Now use extrapolation with N = 20, 40 and find its error. What do you think is the order of the extrapolation method using the trapezoid rule?

2. The left, right and trapezoid rules for approximating a definite integral all have the form

$$Af(x_0) + \sum_{i=1}^{n-1} f(x_i) + Bf(x_n)$$

where the constants A and B depend on the method. For the left rule, A = 1, B = 0. For the right rule, A = 0, B = 1. What are A and B for the trapezoid rule?