

## Sample Exam 1 Solutions– Math 263 (sect 9)

1.

- (a) The percentage of students with under \$10.00 in their possession is C) 44%
- (b) The median is approximately B) \$11
- (c) Distribution is skewed right, so the median will be (ii) to the left of the mean
- (d) Q1 is about 5, Q3 is about 20, so IQR is B) \$15.
- (e) There were 42 students who had between \$10 and \$20 in their possession.

2.

- (a) What proportion of candidates takes more than two hours to learn the computer system?  
 $z = (120 - 90) / 18 = 1.66667$ . From tables or calculator the proportion below this is 0.9522, so the proportion above it is  $1 - 0.9522 = 0.0478 = 4.78\%$
- (b) What proportion of candidates will be hired automatically?  $z = (100 - 90) / 18 = 0.55556$   
Proportion less than this is 0.7107 = 71.07 %
- (c) What is the cut-off time the market research company uses? The slowest typists are the ones with the longest times. So we want the 90<sup>th</sup> percentile for times. For standard normal the 90<sup>th</sup> percentile is at 1.28. So if  $x$  is the cutoff time, then  $1.28 = (x - 90) / 18$ . So  $x = 113$  mins. They won't hire anyone who takes longer than 113 mins.
- (d) The distribution is symmetric about the mean of 90. So 12.5% of the times are less than 75 mins. For the standard normal the  $z$  value below which we have 12.5% is -1.15. This corresponds to time of 75 mins. So if  $s$  is the standard deviation,  $1.15 s = 15$ . So  $s = 13.04$  mins.

3. For the standard normal the 1<sup>th</sup> percentile is at  $z = -2.33$ . This corresponds to a weight of 202g -  $2.33 \times 3g = 195g$

4. (a) What is the median salary of the 20 employees? 48
- (b) What is the first quartile of the 20 salaries? 39
- (c) What is the interquartile range of the 20 salaries?  $60.5 - 39 = 21.5$
- (d)
- A) The median salary would increase by \$3000
  - B) The interquartile range of the salaries would not change. (Both Q1 and Q3 increase by \$3000).
  - C) The standard deviation of the salaries would not change.

- (e) For each of the following sentences, fill in the blank.
- A) The maximum salary is approximately 97,000 dollars.
  - B) The minimum salary is approximately 36,000 dollars.
  - C) The interquartile range is approximately 20,000 dollars.
  - D) Seventy-five percent of the employees in this sample of 20 earn more than approximately 45,000 dollars.

- (f) Based on this boxplot, answer each of the following questions with yes, no, or can't tell.
- A) Is the salary distribution heavily skewed? No, not heavily
  - B) Do about 10 employees make more than \$55,000? Yes, this is approximately the median.
  - C) Does nobody make more than \$71,000? No, there is one person making about \$97,000.
  - D) Is the range of the salaries roughly \$35,000? No, it is roughly \$97,000-\$35,000=\$62,000

5. Match the four graphs labeled A, B, C, and D, with the following four possible values of the correlation coefficient:  $-0.9$ ,  $-0.7$ ,  $0.4$ ,  $0.95$ . Assume all four graphs are made on the same scale.

- A)  $-0.9$
- B)  $0.95$
- C)  $0.4$
- D)  $-0.7$

6. (a)  $r=0.9783$

(b)  $(\text{ACT score}) = 0.01627 \times (\text{SAT score}) - 3.065$

- (c) No, there is a strong correlation, but correlation does not imply causation. A more likely scenario is that there is a lurking variable, for example, the student's intelligence or ability to take these type of tests, that has a casual relation with both of the tests.

(d) Prediction is  $0.01627 \times 1225 - 3.065 = 16.9$

- (e) For every 100 points increase in the students SAT score we expect an increase of 1.627 points in his or her ACT score.