

## Fourier series and transforms - Check your understanding

- Is the Fourier series of  $f$  evaluated at point  $x$  always equal to  $f(x)$ ? Why or why not?
- What is the Gibbs phenomenon?
- Are there functions which do not have a Fourier series? If so, give an example.
- If the forcing applied to an oscillator is not sinusoidal, is it possible to have a resonance? Why or why not?
- If  $f$  is a function of  $x$ ,  $\mathcal{F}$  denotes the Fourier transform, and  $\mathcal{F}^{-1}$  the inverse Fourier transform, is it always true that  $\mathcal{F}^{-1}[\mathcal{F}(f)](x) = f(x)$ ? Why or why not?
- Is the Fourier transform a linear transformation? Why or why not?
- If you are asked to find either the Fourier series or the Fourier transform of a given function  $f$ , how do you decide which transform to write?