Abstract: In this talk we will give a survey of some of the important results in the theory of (finite) groups. In particular we are going to discuss the fundamental questions for representations of groups (as permutations or as invertible matrices). We will then outline, how some of these questions can be answered in a computational/algorithmic way and also discuss applications.