

The following properties of logarithms may be deduced from the properties of exponents:

Properties of Logarithms

Note that $\log x$ and $\ln x$ are not defined when x is negative or 0.

1. $\log(AB) = \log A + \log B$

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2. $\log\left(\frac{A}{B}\right) = \log A - \log B$

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3. $\log(A^p) = p \log A$

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4. $\log(10^x) = x$

4. $\ln e^x = x$

5. $10^{\log x} = x$

5. $e^{\ln x} = x$

In addition, $\log 1 = 0$ because $10^0 = 1$, and $\ln 1 = 0$ because $e^0 = 1$.