

These can save time when doing homework print then cut and paste into your homework, or cut and paste and do the work in word.

## Banzhaf method

*if the number of players are no more than 5 you must write all the coalitions*

If there are **3 players** there are  $2^3 - 1 = 7$  coalitions

$\{P_1\}$	$\{P_1, P_2\}$	$\{P_1, P_2, P_3\}$
$\{P_2\}$	$\{P_1, P_3\}$	
$\{P_3\}$	$\{P_2, P_3\}$	

If there are **4 players** there are  $2^4 - 1 = 15$  coalitions

$\{P_1\}$	$\{P_1, P_2\}$	$\{P_1, P_2, P_3\}$	$\{P_1, P_2, P_3, P_4\}$
$\{P_2\}$	$\{P_1, P_3\}$	$\{P_1, P_2, P_4\}$	
$\{P_3\}$	$\{P_1, P_4\}$	$\{P_1, P_3, P_4\}$	
$\{P_4\}$	$\{P_2, P_3\}$	$\{P_2, P_3, P_4\}$	
	$\{P_2, P_4\}$		
	$\{P_3, P_4\}$		

If there are **5 players** there are  $2^5 - 1 = 31$

$\{P_1\}$	$\{P_1, P_2\}$	$\{P_1, P_2, P_3\}$	$\{P_1, P_2, P_3, P_4\}$	$\{P_1, P_2, P_3, P_4, P_5\}$
$\{P_2\}$	$\{P_1, P_3\}$	$\{P_1, P_2, P_4\}$	$\{P_1, P_2, P_3, P_5\}$	
$\{P_3\}$	$\{P_1, P_4\}$	$\{P_1, P_2, P_5\}$	$\{P_1, P_2, P_4, P_5\}$	
$\{P_4\}$	$\{P_1, P_5\}$	$\{P_1, P_3, P_4\}$	$\{P_1, P_3, P_4, P_5\}$	
$\{P_5\}$	$\{P_2, P_3\}$	$\{P_1, P_3, P_5\}$	$\{P_2, P_3, P_4, P_5\}$	
	$\{P_2, P_4\}$	$\{P_1, P_4, P_5\}$		
	$\{P_2, P_5\}$	$\{P_2, P_3, P_4\}$		
	$\{P_3, P_4\}$	$\{P_2, P_3, P_5\}$		
	$\{P_3, P_5\}$	$\{P_2, P_4, P_5\}$		
	$\{P_4, P_5\}$	$\{P_3, P_4, P_5\}$		

## Shapley-Shubik method

If there are **3 players**

These are the list of coalition  $3! = 6$  coalitions

$\langle P_1, P_2, P_3 \rangle$	$\langle P_2, P_1, P_3 \rangle$	$\langle P_3, P_1, P_2 \rangle$
$\langle P_1, P_3, P_2 \rangle$	$\langle P_2, P_3, P_1 \rangle$	$\langle P_3, P_2, P_1 \rangle$

If there are **4 players**

These are the list of coalitions  $4! = 24$  coalitions

$\langle P_1, P_2, P_3, P_4 \rangle$	$\langle P_2, P_1, P_3, P_4 \rangle$	$\langle P_3, P_1, P_2, P_4 \rangle$	$\langle P_4, P_1, P_2, P_3 \rangle$
$\langle P_1, P_2, P_4, P_3 \rangle$	$\langle P_2, P_1, P_4, P_3 \rangle$	$\langle P_3, P_1, P_4, P_2 \rangle$	$\langle P_4, P_1, P_3, P_2 \rangle$
$\langle P_1, P_3, P_2, P_4 \rangle$	$\langle P_2, P_3, P_1, P_4 \rangle$	$\langle P_3, P_2, P_1, P_4 \rangle$	$\langle P_4, P_2, P_1, P_3 \rangle$
$\langle P_1, P_3, P_4, P_2 \rangle$	$\langle P_2, P_3, P_4, P_1 \rangle$	$\langle P_3, P_2, P_4, P_1 \rangle$	$\langle P_4, P_2, P_3, P_1 \rangle$
$\langle P_1, P_4, P_2, P_3 \rangle$	$\langle P_2, P_4, P_1, P_3 \rangle$	$\langle P_3, P_4, P_1, P_2 \rangle$	$\langle P_4, P_3, P_1, P_2 \rangle$
$\langle P_1, P_4, P_3, P_2 \rangle$	$\langle P_2, P_4, P_3, P_1 \rangle$	$\langle P_3, P_4, P_2, P_1 \rangle$	$\langle P_4, P_3, P_2, P_1 \rangle$