

## MATH 323 Section 2

### QUIZ 4

February 25<sup>th</sup>, 2013

Your Name: \_\_\_\_\_

Let  $A$  be the following set:

$$A = \{a, b, c, d, e, f\}.$$

Suppose  $R$  is an equivalence relation on  $A$ , and let  $E_a$  denote the equivalence class of  $a$ ,  $E_b$  denote the equivalence class of  $b$ , etc. For each of the following, explain why the statement is true (using properties of equivalence relations).

- a) We must have  $bRb$ .
- b) If  $aRd$  and  $dRf$  then the equivalence class of  $a$  contains both  $d$  and  $f$ .
- c) If  $a$  is in the equivalence class of  $b$  then  $E_b = E_a$ .

a) This is the reflexive property.

b) Since  $aRd$ , we have that  $d \in E_a$ . Using transitivity, since  $aRd$  and  $dRf$ , we have  $aRf$ , so  $f \in E_a$ .

c) If  $a \in E_b$ , then  $aRb$  and, by transitivity, if  $cRa$ , then  $cRb$  and so  $E_a \subseteq E_b$ . Similarly, since  $aRb$ , symmetry says that  $bRa$ , and by the same transitivity argument,  $E_b \subseteq E_a$ .