## Complex Numbers

Concept tests

Every nonnegative real number has a real square root

1. True
2. False

For any complex number $z$, the product $z \cdot \bar{z}$ is a real number
, 1. True
2. False


It is possible for a function of a complex variable to be multi-valued
, 1. True
2. False


The square of any complex number is a real number

1. True
, 2. False

If $f$ is a polynomial and $f(z)=i$, then $f(\bar{z})=i$

1. True
, 2. False



If $z=x+i y$, where $x$ and $y$ are positive, then $z^{2}=a+i b$ has $a$ and $b$ positive.

1. True
$\checkmark$ 2. False

2. True
3. False
.

Every nonzero complex number z can be written in the form $\mathrm{z}=\mathrm{e}^{\mathrm{w}}$, where w is another complex number.

Which of the statements below describes the region of the complex plane corresponding

$$
\text { to }|z-i| \leq 9 \text { ? }
$$

1. The circle of radius 3 centered at i
2. The disk of radius 9 centered at the origin
3. The disk of radius 9 centered at i


If z is a complex number, then $\mathrm{e}^{\mathrm{iz}}$ has modulus 1

1. True
$\checkmark$ 2. False

The product of two analytic functions is analytic

1. True
2. False


Any solution of the equation $\mathrm{z}^{4}-16=0$ may be written in the form $\mathrm{z}=2 \mathrm{w}$, where w is a
fourth root of unity

1. True
2. False


The curve of equation $e^{(a+i b) t}$, where $a$ and $b$ are given real numbers and $t$ varies in [ 0,1 ], is a piece of a spiral in the complex plane
, 1. True
2. False

The curve of equation $e^{a+i b}$, where $a$ and $b$ are real numbers, a varies and $b$ is fixed, is a straight line in the complex plane

1. True
2. False



If a function has a limit as $z \rightarrow z_{0}$, then the limit does not depend on the path followed
by z as it approaches $\mathrm{z}_{\mathrm{o}}$

1. True
$\checkmark$ 2. False
2. True
3. False


Is the function $|\mathrm{z}|^{2}$ entire?

1. Yes
, 2. No


The function $|z|^{2}$ is analytic at the origin

1. True
, 2. False

2. True
3. False

The graph below shows the modulus of a function of a complex variable $f(z)$. Is $f$ entire?


1. Yes
2. No
3. Not enough information to decide


The graph below shows a contour plot of two functions $u(x, y)$ and $v(x, y)$. Is the function $f(z)=u(x, y)+i v(x, y)$ analytic?

1. Yes

V2. No

3. Not enough information to decide

